

Chapter 5 Floating-Point Operations

Although the MPC-2000 series can handle floating-point operations, in order to distinguish them from general control operations, floating-point operations are executed only by the independent FLOAT command and the following macro commands.

5-1 Floating-Point Arithmetic Macro Commands

Macro commands are commands used for position corrections in image processing. Because the AFFIN command can rotate two-dimensional vectors, it can efficiently perform coordinate corrections. For the details, see Command Reference.

AFFIN	Rotational conversion of point data
ATAN	Obtaining an angle with ATAN
ATAN2	Obtaining an angle with ATAN (General use)
COS	COS arithmetic
SIN	SIN arithmetic
TAN	TAN arithmetic
GETDG	Angle formed by a line connecting two points and the X axis

5-2 Floating-Point Arithmetic Operations

Double-precision array variable (FP(n))

FP(n) is a special array variable. Eight of them, FP(0)~FP(7), are prepared, and can be used as floating-point arithmetic compatible variables. Examples are shown below. When a formula which substitutes FP(n) is described, the formula becomes a floating-point arithmetic formula, and data are stored in FP(n) in a floating-point format unlike ordinary variables.

- Display a numerical value directly in the E format.

```
#FP(1)=10/3
#pr FP(1)
3.333333E+00
#
```

- Multiply by 10000, convert into an integer, and display.

```
#FP(1)=10/3
#pr FP(10000,1)
33333
#
```

- Calculation of Napier's constant

```
10 FLOAT FP(2)=1
15 a=1
20 FOR i=1 TO 100
30 a=a*i
40 FLOAT FP(2)=FP(2)+1/a
50 NEXT
70 FORMAT "0.0000"
80 PRINT STR$(FP(10000,2))
#run
```

```
2.7182
#
```

- Solution of a quadratic equation $x^2 + 4x + 3 = 0$

```
10 a=1 : b=4 : c=3
20 FLOAT FP(0)=(SQR(b*b-(4*a*c))-b)/2/a
30 FLOAT FP(1)=(SQR(b*b-(4*a*c))*-1-b)/2/a
40 PRINT FP(10000,0) FP(10000,1)
#run

-10000 -30000
#
```

FLOAT command

MPC-2000 series arithmetic operations ordinarily deal with integers. In order to distinguish these operations, a FLOAT command is prepared. When FP(n) is specified as a substituted variable, the FLOAT command is automatically added to the arithmetic formula. Arithmetic operations in the FLOAT command prioritize multiplication (*) and division (/) over addition and subtraction in the same manner as in ordinary arithmetic formulas.

Examples:

[Example of a FLOAT command being added]

```
#10 fp(2)=1/3
list
10   FLOAT FP(2)=1/3
#
```

[Example of prioritizing multiplication]

```
10   FLOAT a=SQR(3*3+4*4)
20   PRINT a
#run

5
#
```

When a substituted variable is an ordinary integer variable, if a FLOAT command is added, the result is that although substitution occurs as an integer, the internal arithmetic becomes a floating-point operation. Along with this, the square root function SQR() also becomes a floating-point arithmetic operation.

```
10   FLOAT a=SQR(3)*10000000
20   PRINT a
#run

17320508
#
```

Floating-point compatible functions

Arithmetic functions which can be used in a FLOAT command are as follows. These functions are regarded as double-precision floating-point functions in a FLOAT command. Their behavior differs from those in an ordinary integer arithmetic formulae.

SQR	Square root calculation	
SQ	Square calculation	
SIN	Trigonometric function SIN	Input is in radians.
COS	Trigonometric function COS	Input is in radians.
TAN	Trigonometric function TAN	Input is in radians.
ATAN	Trigonometric function ATAN	Output is in radians.
ACOS	Trigonometric function ACOS	Output is in radians.
RAD	Conversion from degree to radian	Output is in radians.
DEG	Conversion from radian to degree	Output is in degrees.
VAL	Obtain a character string as a floating-point value.	

Illustrated below is an example showing that the square sum of SIN and COS of an arbitrary angle integer i is 1.

Because the arguments of SIN and COS are in radians, an integer value of 100 degrees is converted to radians with an RAD() function.

```
10   FLOAT a=SQR(SQ(SIN(RAD(i)))+SQ(COS(RAD(i))))*1000000
20   PRINT a
#i=100
#run

1000000
#
```

Further, π is calculated using ATAN.
 Because $\text{TAN}(45 \text{ degrees}) = 1$, $\text{ATAN}(1)$ becomes $\pi/4$ in radians.

```
10  FLOAT  FP(0)=ATAN(1)*4
20  PRINT  FP(10000,0)
#run
```

```
31415
#
```

In order to obtain the value of π itself, the following is a short-cut.

```
10  FLOAT  FP(5)=RAD(180)
20  PRINT  FP(5)
#run
```

```
3.141593E+00
#
```

In actual applications, there are cases where floating-point numbers in EXP expression from external equipment are incorporated. For this, the VAL function is used.

The VAL function becomes a floating-point function in a FLOAT command and can read character strings of a type, $\pm X.XXXXXXE(e)YYY$

```
10  a$="C41$=Mx+9.7042e+002 C42$=My-6.3210e+002 "
20  FLOAT  a=VAL(a$) FP(0)=VAL(0) b=VAL(0) FP(1)=VAL(0)
30  PRINT  a FP(0) b FP(1)
#run
```

```
41 9.704200E+02 42 -6.321000E+02
#
```

For conversion of $\text{FP}(n)$ into a character string, $\text{FP}\$(n)$ is used.

Illustrated below is an expression of $\text{FP}\$(n)$ and the fixed-point format of its integer-converted value.

```
10  FLOAT  FP(5)=RAD(180)
20  PRINT  FP$(5)
25  FLOAT  A=FP(5)*1000000
30  FORMAT "0.000000"
40  PRINT  STR$(A)
#run
```

```
3.141593E+00
3.141592
#
```

Speed of floating-point arithmetic operations

The speed of a floating-point arithmetic operation is evaluated as follows:

```
LIST
95  SYSCLK=0
100 FOR i=1 TO 1000
110  FLOAT  FP(0)=DEG(ATAN(5/100))
120  NEXT
130  PRINT  SYSCLK
140  PRINT  FP(0)
#run 95
95-
707
```

```
2.862405E+00  
#
```

In this example, one ATAN calculation and the conversion into an angle took 707 m seconds. Next, an example of complex arithmetic is executed.

```
LIST  
10  SYSCLK=0  
20  FOR i_=1 TO 180  
30  FLOAT a_=SQR(SQ(SIN(RAD(i_)))+SQ(COS(RAD(i_))))  
40  IF a_!=1 THEN :PRINT "FL_NG " :END :END_IF  
50  NEXT  
60  PRINT SYSCLK  
#run  
  
145  
#
```

The complex arithmetic took $145/180 = 0.806 \rightarrow 806 \mu$ seconds.

* $66/180 = 0.366 \rightarrow 366 \mu$ seconds in MPC-2200 case.

Because complicated floating-point operations take a long time, they should be used in complex arithmetic applications after evaluating the time it takes.